

C.U.SHAH UNIVERSITY

Summer Examination-2018

Subject Name : Advanced Mathematics

Subject Code : 2TE02AMT2

Branch: Diploma (All)

Semester : 2

Date : 25/04/2018

Time : 10:30 To 01:30

Marks : 70

Instructions:

- (1) Use of Programmable calculator & any other electronic instrument is prohibited.
- (2) Instructions written on main answer book are strictly to be obeyed.
- (3) Draw neat diagrams and figures (if necessary) at right places.
- (4) Assume suitable data if needed.

Q-1

Attempt the following questions:

(14)

a) $\lim_{x \rightarrow 0} \frac{a^x - 1}{x} = \underline{\hspace{2cm}}$

- (A) $\log_a e$ (B) $\log_e a$ (C) e (D) 1

b) $\lim_{x \rightarrow 1} \frac{x^3 - 1}{x - 1} = \underline{\hspace{2cm}}$

- (A) -1 (B) 1 (C) 0 (D) 3

c) $\lim_{x \rightarrow 0} \frac{\tan x}{x} = \underline{\hspace{2cm}}$

- (A) -1 (B) 0 (C) 1 (D) None of these

d) $\frac{d(7)}{dx} = \underline{\hspace{2cm}}$

- (A) 0 (B) 1 (C) -1 (D) 7x

e) $\frac{d\left(\frac{1}{x}\right)}{dx} = \underline{\hspace{2cm}}$

- (A) $\frac{1}{x}$ (B) $-\frac{1}{x^2}$ (C) $\log x$ (D) $-\frac{1}{x}$

f) $\frac{d(\sin^{-1} x)}{dx} = \underline{\hspace{2cm}}$

- (A) $\frac{-1}{\sqrt{1-x^2}}$ (B) $\frac{1}{\sqrt{1-x^2}}$ (C) $\frac{1}{1+x^2}$ (D) $\frac{-1}{1+x^2}$

If $f(x) = \log \sqrt{x^2 + 1}$ then $f'(0) = \underline{\hspace{2cm}}$.

g) $\int \frac{1}{2} dx = \underline{\hspace{2cm}}$

- (A) $\frac{1}{2}$ (B) 1 (C) 2 (D) 0

h) $\int a^x dx = \underline{\hspace{2cm}}$



(A) $\frac{a^x}{\log_e a} + c$ (B) $a^x \log_e a + c$ (C) $a^x + c$ (D) $\log_e a + c$

i) $\int \frac{1}{\sqrt{a^2 - x^2}} dx = \underline{\hspace{2cm}}$

(A) $\cot^{-1} \frac{x}{a} + c$ (B) $\tan^{-1} \frac{x}{a} + c$ (C) $\cos^{-1} \frac{x}{a} + c$ (D) $\sin^{-1} \frac{x}{a} + c$

j) $\int_0^1 x dx = \underline{\hspace{2cm}}$

(A) 1 (B) 2 (C) $\frac{1}{2}$ (D) None of these

k) $|(2, 1, 1) + (1, 2, 3)| = \underline{\hspace{2cm}}$.

(A) 10 (B) $\sqrt{43}$ (C) $\sqrt{34}$ (D) None of these

l) $(1, 1, 1) \cdot (-1, 2, -3) = \underline{\hspace{2cm}}$.

(A) -2 (B) 2 (C) 1 (D) -1

m) $(2, -1, 3) \times (-4, 2, -6) = \underline{\hspace{2cm}}$.

(A) $(-8, -2, -18)$ (B) $(8, 2, 18)$ (C) $(0, 0, 0)$ (D) None of these

n) If the two vectors \vec{a} and \vec{b} are perpendicular (orthogonal) then $\vec{a} \cdot \vec{b} = \underline{\hspace{2cm}}$.

(A) 0 (B) 1 (C) -1 (D) None of these

Attempt any four questions from Q-2 to Q-8

Q-2

Attempt all questions

(14)

a) If $\vec{a} = 3i - j - 4k$, $\vec{b} = -2i + 4j - 3k$ and $\vec{c} = -i + 2j - 5k$ then find $|\vec{a} + 2\vec{b} - \vec{c}|$. **(5)**

b) Find unit vector which is perpendicular to $\vec{a} = 5i + 7j - 2k$ and $\vec{b} = j - 2k + 3i$. **(5)**

c) Evaluate: $\lim_{\theta \rightarrow 0} \frac{\cos \theta - \cot \theta}{\theta}$ **(4)**

Q-3

Attempt all questions

(14)

a) Prove that $\lim_{x \rightarrow \infty} \left[\sqrt{x} (\sqrt{x+p} - \sqrt{x}) \right] = \frac{p}{2}$. **(5)**

b) Evaluate: $\lim_{x \rightarrow (-2)} \frac{x^3 + 2x^2 + x + 2}{x^2 + x - 2}$ **(5)**

c) Find $\frac{dy}{dx}$ if $y = \frac{1 + \sin x}{1 - \sin x}$. **(4)**

Q-4

Attempt all questions

(14)

a) The equation of motion of a particle is $S = 2t^3 + 3t^2 - 12t + 5$. **(5)**
 (i) Find velocity at $t = 0$. (ii) Find acceleration at $t = 1$.

b) Find $\frac{dy}{dx}$ if $y = \log \left[x + \sqrt{x^2 + a^2} \right]$. **(5)**

c) If $\vec{a} = (2, -3, -1)$ and $\vec{b} = (1, 4, -3)$ then find $(\vec{a} + \vec{b}) \times (\vec{a} - \vec{b})$. **(4)**



